



# LOYOLA COLLEGE (AUTONOMOUS), CHENNAI – 600 034

B.Sc. & B.C.A. DEGREE EXAMINATION – STATS, PHY., CHE., COMPU. SCI., APPLI.

THIRD SEMESTER – NOVEMBER 2015

## MT 3206 - APPLIED MATHEMATICS

Date : 12/11/2015

Dept. No.

Max. : 100 Marks

Time : 09:00-12:00

### PART - A

ANSWER ALL QUESTIONS

10 X 2 = 20

- 1) Define a revenue function.
- 2) Write any two properties of definite integrals.
- 3) Define divergence and curl of a vector function.
- 4) Show that  $\vec{F} = z\hat{i} + x\hat{j} + y\hat{k}$  is solenoidal.
- 5) Write any two applications of differential equations.
- 6) Define mixture problem.
- 7) Find  $L(e^{2t})$ .
- 8) If  $L(f(t)) = F(s)$  then  $L(e^{-at}f(t)) = \underline{\hspace{2cm}}$
- 9) Find  $L^{-1}\left(\frac{1}{s^2+4}\right)$ .
- 10) Define Spearman's rank correlation coefficient.

### PART - B

ANSWER ANY FIVE QUESTIONS

5 X 8 = 40

- 11) The cost function of a firm is  $C = 300x - 10x^2 + \frac{1}{3}x^3$  where C is the cost and x is the output. (i) Find output at which marginal cost is minimum. (ii) Find output at which average cost is equal to marginal cost.
- 12) Evaluate  $\iint e^{\frac{y}{x}} dx dy$  over the region bounded by the straight lines  $y = x$ ;  $y = 0$  and  $x = 1$ .
- 13) Find the values of  $a, b, c$  so that the vector  $\vec{F} = (x + 2y + az)\hat{i} + (bx - 3y - z)\hat{j} + (4x + cy + 2z)\hat{k}$  is irrotational.
- 14) If  $\vec{F} = x^2\hat{i} + xy\hat{j}$  evaluate  $\int \vec{F} \cdot d\vec{r}$  along the line  $y = x$  from (0,0) to (1,1).
- 15) Evaluate  $\int_0^{\infty} e^{-2t} \sin 3t dt$ .
- 16) Find  $L^{-1}\left(\frac{1}{s(s+1)(s+2)}\right)$ .

17) A tank contains 100 gallon brine in which 10 lb of salt dissolved. Brine contains 2 lb salt per gallon flows into the tank at 5 gal/min. If the well-stirred mixture is drawn of at 4 gal/min. Find (i) the amount of salt in the tank at time  $t$ , and the amount of salt in the tank at  $t = 10$  min.

18) From the following data calculate the coefficient of correlation.

|   |    |    |    |    |    |
|---|----|----|----|----|----|
| X | 1  | 2  | 3  | 4  | 5  |
| Y | 10 | 20 | 30 | 50 | 40 |

**PART - C**

**ANSWER ANY TWO QUESTIONS**

**20 X 2 = 40**

19) a) Determine consumer surplus and producer surplus under pure competition for the demand function

$p = 36 - x^2$  and supply function  $p = 6 + \frac{x^2}{4}$  where  $p$  is the price and  $x$  is the quantity.

b) Evaluate  $\int_0^a \int_0^{\sqrt{a^2-x^2}} y^3 dy dx$ . ( 12 + 8 )

20 a) If  $\vec{F} = x^2 y \hat{i} + y^2 z \hat{j} + z^2 x \hat{k}$ , find  $\text{curl } \text{curl } \vec{F}$ .

b) If  $\vec{F} = (3x^2 + 6y) \hat{i} - 14yz \hat{j} + 20xz^2 \hat{k}$ , evaluate  $\int \vec{F} \cdot d\vec{r}$  along the line joining the points (0,0,0) to (1,1,1). ( 10 + 10 )

21a) Find  $L^{-1} \left( \log \frac{s+1}{s-1} \right)$ .

b) Solve  $\frac{d^2 y}{dt^2} + 2 \frac{dy}{dt} - 3y = \sin t$  given that  $y = \frac{dy}{dt} = 0$  when  $t = 0$ . ( 8 + 12 )

22 a) In a culture of east, the amount A of active yeast grows at a rate proportional to the amount present. If the original amount  $A_0$  doubles in 2 hours, how long does it for the original amount to triple?

b) From the following data calculate mean standard deviation, coefficient of variation and variance by assumed mean method.

|                 |      |       |       |       |       |       |
|-----------------|------|-------|-------|-------|-------|-------|
| Marks           | 0-10 | 10-20 | 20-30 | 30-40 | 40-50 | 50-60 |
| No of students. | 10   | 20    | 30    | 50    | 40    | 30    |

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